

Substitution Method

Use this method when the coefficient of one of the variables is 1.

~~$x + y = 4$~~

$$x = -y + 4$$

$$2x - y = -1$$

$$2(-y + 4) - y = -1$$

$$-2y + 8 - y = -1$$

$$-3y = -9$$

$$y = 3$$

$$x = -3 + 4 = 1$$

$(1, 3)$

~~$x + y = 3$~~

$$2x + 2y = -4$$

$$y = -x + 3$$

$$2x + 2(-x + 3) = -4$$

$$2x - 2x + 6 = -4$$

$$6 = -4$$

NO
SOLUTION

Substitution Method

$$6x + 5y = 1$$

~~$$x - 3y = 4$$~~

$$x = 3y + 4$$

$$6(3y + 4) + 5y = 1$$

$$18y + 24 + 5y = 1$$

$$23y = -23$$

$$y = -1$$

$$x = 3(-1) + 4 = +1$$

$$(1, -1)$$

$$y = \frac{1}{2}x + 4$$

$$2y = 2x + 8$$

$$2\left(\frac{1}{2}x + 4\right) = 2x + 8$$

$$x + 8 = 2x + 8$$

$$0 = x$$

$$y = \frac{1}{2}(0) + 4 = 4$$

$$(0, 4)$$

Addition/Subtraction Method

Use this method when the coefficient of the like terms are equal. Then add the equations so one of the variables is eliminated.

$$\begin{array}{r} x + y = 5 \\ + 2x - y = 7 \\ \hline 3x = 12 \\ x = 4 \end{array}$$

$$\begin{array}{r} 4 + y = 5 \\ y = 1 \\ (4, 1) \end{array}$$

$$\begin{array}{r} x + 4y = 10 \\ -(x + 2y = 6) \\ \hline 2y = 4 \\ y = 2 \end{array}$$

$$\begin{array}{r} x + 2(2) = 6 \\ -4 \quad \quad 4 \\ \hline x = 2 \end{array} \quad (2, 2)$$

Multiplication/ Elimination Method

Multiply one equation by a number(s) so that when you add the equations, the sum will result in eliminating one variable.

$$2(4x + y = 6)$$

$$\begin{array}{r} 3x + 2y = 7 \\ - (8x + 2y = 12) \\ \hline -5x = -5 \\ x = 1 \end{array}$$

$$\begin{array}{l} 4(1) + y = 6 \\ y = 2 \end{array} \quad (1, 2)$$

$$\begin{array}{r} 2(3x - 4y = 8) \rightarrow 6x - 8y = 16 \\ 3(2x + 3y = 9) \rightarrow 6x + 9y = 27 \\ \hline -17y = -11 \\ y = \frac{11}{17} \end{array}$$

$$\begin{array}{r} 9x - 12y = 24 \\ + 8x + 12y = 36 \\ \hline 17x = 60 \\ x = \frac{60}{17} \end{array}$$

$$\begin{array}{l} 3x - 4\left(\frac{11}{17}\right) = 8 \\ \rightarrow 3x - \frac{44}{17} = 8 \\ 51x - 44 = 136 \end{array}$$

$$\begin{array}{r} 51x = 180 \\ \frac{51}{51} \\ x = \frac{60}{17} \end{array}$$

EXAMPLE 8 MODELING - *When Are Repair Costs the Same?*

Melinda Melendez needs to purchase a new radiator for her car and have it installed by a mechanic. She is considering two garages: Steve's Repair and Greg's Garage. At Steve's Repair, the parts cost \$200 and the labor cost is \$50 per hour. At Greg's Garage, the parts cost \$375 and the labor cost is \$25 per hour. How many hours would the repair need to take for the total cost at each garage to be the same?

$$\begin{aligned}
 C &= 200 + 50h \\
 C &= 375 + 25h \\
 375 + 25h &= 200 + 50h \\
 &\quad -200 \\
 175 + 25h &= 50h \\
 \frac{175}{25} &= \frac{25h}{25} \\
 7 &= h
 \end{aligned}$$

EXAMPLE 9 MODELING - *A Mixture Problem*

Pat Kuby, a pharmacist, needs 500 milliliters (mℓ) of a 10% phenobarbital solution. She has only a 5% phenobarbital solution and a 25% phenobarbital solution available. How many milliliters of each solution should she mix to obtain the desired solution?

$$\begin{aligned}
 &.25(f + t = 500) \\
 &.05f + .25t = .10(500) \\
 - &.25f + .25t = 125 \\
 \hline
 &-.20f = -75 \\
 &\quad \underline{-.20} \\
 &f = 375 \\
 &t = 125
 \end{aligned}
 \qquad
 \begin{aligned}
 f &= 5\% \\
 t &= 25\%
 \end{aligned}$$

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45. **MODELING - Chemical Mixture** Antonio Gonzalez is a chemist and needs 10 liters (ℓ) of a 40% hydrochloric acid solution. He discovers he is out of the 40% hydrochloric acid solution and does not have sufficient time to reorder. He checks his supply shelf and finds he has a large supply of both 25% and 50% hydrochloric acid solutions. He decides to use the 25% and 50% solutions to make 10 ℓ of a 40% solution. How many liters of the 25% solution and of the 50% solution should he mix?

$$\begin{array}{r} \sim (t + f = 10) \\ .25t + .50f = .40(10) \\ - (.25t + .25f = 2.5) \\ \hline .25f = 1.5 \\ \frac{.25f}{.25} = \frac{1.5}{.25} \\ f = 6 \quad t = 4 \end{array}$$

$$\begin{array}{l} t = .25 \\ f = .50 \end{array}$$

46. **MODELING - Sets of Dishes** A restaurant manager purchased 100 sets of dishes. One design cost \$30 per set, and another design cost \$40 per set. If the manager spent \$3200 on the dishes, how many sets of each design did she purchase?

$$\begin{array}{r} 30(t + f = 100) \\ 30t + 40f = 3200 \\ - 30t + 30f = 3000 \\ \hline 10f = 200 \\ f = 20 \quad t = 80 \end{array}$$

$$\begin{array}{l} t = 30 \\ f = 40 \end{array}$$

Bobby Llama needs 400 liters of a 60% mustache enhancement solution. He discovers that he only has a 20% solution and a 90% solution available. How many liters of each solution should Bobby mix to obtain the desired solution.